

**H. Algebra II Semester II Review**  
**Part 9 – Trigonometric Identities and Logarithm Rules**

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**9.a Applying Angle Sum/Difference and Double Angle Identities for Evaluation**

Evaluate the following trigonometric functions without using a calculator.

1.  $\sin\left(\frac{13\pi}{12}\right)$

2.  $\cos\left(\frac{5\pi}{8}\right)$

Review the angle sum/difference and double angle identities for sine and cosine

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**9.b Evaluation of Related Angles using Double Angle Identities**

Given that  $\tan \theta = -\frac{1}{4}$  and  $\frac{\pi}{2} < \theta < \pi$ , evaluate the each trigonometric function without using a calculator.

1.  $\sin \theta$

3.  $\sin 2\theta$

2.  $\cos \theta$

4.  $\cos 2\theta$

5.  $\tan 2\theta$

Use the double angle sine and cosine identities. Recall that sine and cosine have a range of -1 to 1 and should never exceed those values.

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**9.c Properties of Logarithms**

Expand each expression using properties of logarithms.

1.  $\log(x \cdot \sqrt[3]{1-x})$

2.  $\log_5\left(\frac{x^2}{y \cdot z^3}\right)$

3.  $\ln\left(\frac{4x^3}{y^2(x-1)^5}\right)$

Condense each expression using properties of logarithms.

4.  $3 \log 2 + 2 \log x - \frac{1}{2} \log(x+4)$

5.  $2 \log_5(x-1) - \log_5(x^2-1)$

6.  $\ln(a-b) + \ln(a+b) - 2 \ln(c) - \ln(d)$

The properties of logarithms are produced from the properties of exponents and have similarities.