

## H. Algebra II Semester II Review

### Part 6 - Inverse Functions

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#### 6.a Analytic Definition of Inverse Functions

Determine whether the following pairs of functions are inverse.

1.  $f(x) = \frac{x+2}{x-5}$

$$g(x) = \frac{5x+2}{x-1}$$

2.  $f(x) = \frac{5}{x-2}$

$$g(x) = \frac{x-2}{5}$$

Find the inverse of each function.

3.  $f(x) = 5 + \sqrt{x+1}$

4.  $f(x) = \sqrt{\frac{x}{3}} - 6$

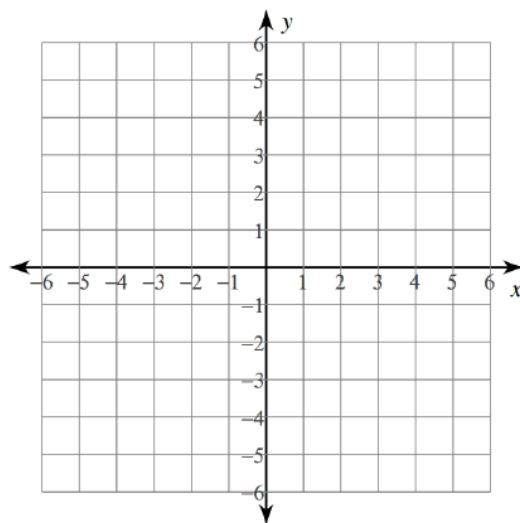
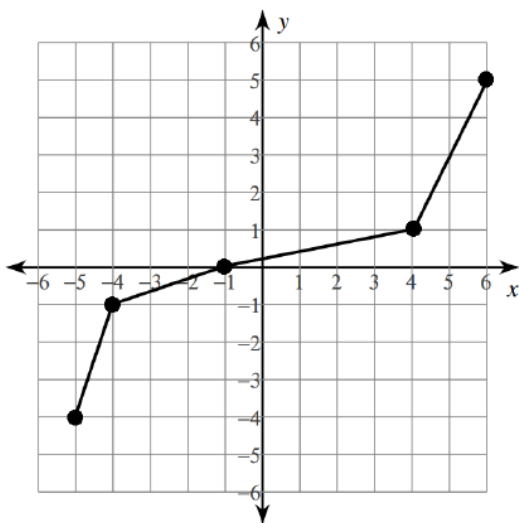
5.  $f(x) = \frac{x-3}{x+2}$

6.  $f(x) = \sqrt[5]{x^3} = x^{3/5}$

Review the definition of inverse functions (it is a pair of equations), the conditions for existence of an inverse function and the procedure for finding an inverse.

#### 6.b Characteristics of Inverse Functions

Use the graph of the following function to generate a graph of its inverse function on the right.



Recall that if  $f(a)=b$  then  $f^{-1}(b)=a$ . This also means that if the graph of  $f(x)$  contains the point  $(a,b)$  then the graph of  $f^{-1}(x)$  contains the point  $(b,a)$ . Because of this, a graph showing both  $f(x)$  and  $f^{-1}(x)$  should appear to be reflected about the line  $y=x$ .