



$$P_n(x) = a_0 + a_1x + a_2x^2 \dots + a_nx^n$$

$$P_n(x) = \underline{a_0} + \underline{a_1}(x-c) + \underline{a_2}(x-c)^2 + \dots + \underline{a_n}(x-c)^n$$

$$f(x) \approx P_n(x)$$

$$P_0(x) = a_0; \quad \underline{a_0 = f(c)}$$

$$P_1(x) = a_0 + a_1(x-c); \quad \underline{a_1 = f'(c)}; \quad P(c) = f(c); \quad \underline{P_1(c) = a_0 = f(c)}$$

$$P_2(x) = a_0 + a_1(x-c) + a_2(x-c)^2$$

$$\textcircled{2} P_2''(c) = f''(c), \quad \textcircled{1} P_2'(c) = f'(c), \quad \textcircled{0} P_2(c) = f(c)$$

$$P_2' = 0 + a_1 + 2a_2(x-c); \quad P_2'(c) = a_1$$

$$P_2'' = 0 + 2a_2; \quad P_2''(c) = \underline{2a_2}$$

$$P_2(c) = a_0$$

$$\underline{a_0 = f(c)}; \quad \underline{a_1 = f'(c)}; \quad 2a_2 = f''(c) \Rightarrow \underline{a_2 = \frac{f''(c)}{2}}$$

$$P_3(x) = a_0 + a_1(x-c) + a_2(x-c)^2 + a_3(x-c)^3$$

$$\textcircled{0} P_3(c) = f(c) \quad \textcircled{1} P_3'(c) = f'(c) \quad \textcircled{2} P_3''(c) = f''(c) \quad \textcircled{3} P_3^{(3)}(c) = f^{(3)}(c)$$

$$P_3'(x) = 0 + a_1 + 2a_2(x-c) + 3a_3(x-c)^2 \quad | \quad a_0 = f(c) \quad \leftarrow$$

$$P_3'(c) = a_1$$

$$P_3''(x) = 0 + 2a_2 + 2 \cdot 3 \cdot a_3(x-c) \quad | \quad a_1 = f'(c) \quad \leftarrow$$

$$| \quad a_2 = \frac{f''(c)}{2} \quad \leftarrow$$

$$P_3''(c) = 2a_2$$

$$| \quad a_3 = \frac{f^{(3)}(c)}{3!} \quad \leftarrow$$

$$P_3^{(3)}(x) = 0 + 2 \cdot 3 \cdot a_3$$

$$| \quad a_3 = \frac{f^{(3)}(c)}{3!} \quad \leftarrow$$

$$P_3^{(3)}(c) = \underline{2 \cdot 3 \cdot a_3} \\ \underline{3!}$$